Write your name below. This exam is worth 100 points. On each problem, you must show all your work to receive credit on that problem. You are allowed to use one page of notes. You cannot collaborate on the exam or seek outside help, nor can you use the recorded lectures, a calculator, any computational software, or material you nd online.

Name:

1. (10 points, 2 each) If the statement is always true then write **TRUE**; if it is possible for the statement to be false then write **FALSE**

- 2. (20 points) A linear transformation L : \mathbb{R}^3 / \mathbb{R}^2 is represented in the standard basis by $A = 1 \quad 3 \quad 0 \quad 5 \quad 1 \quad 4$

 - (a) Find the matrices S

5. (25 points) Let *A* be the matrix with the Singular Value Decomposition given by

$$A = \begin{bmatrix} 0 & 2 = p \\ p \\ 1 = p$$

- (a) (3 points) What is the rank of A?
- (b) (3 points) Is A singular or nonsingular?
- (c) (9 points) Find the best rank 1 approximation of A.
- (d) (10 points) find the pseudoinverse of A and use it to calculate the least squares solution to Ax = b

where $b = \begin{bmatrix} 1 \\ 0 \\ 1 \end{bmatrix} \begin{bmatrix} 1 \\ 2 \\ 1 \\ 1 \end{bmatrix}$