This exam is worth 150 points and has 6 problems.

Show all work and simplify your answers! Answers with no justification will receive no points unless otherwise noted.

## Please begin each problem on a new page.

**DO NOT** leave the exam until you have satisfactorily scanned and uploaded your exam to Gradescope.

You are taking this exam in a proctored and honor code enforced environment. **NO** calculators, cell phones, or other electronic devices or the internet are permitted during the exam. You are allowed one 8.5" **NO** calculators, cell phones, or other electronic 11" crib sheet with writing on two sides.

Remote students are allowed use of a computer during the exam only for a live video of their hands and face and to view the exam in the Zoom meeting.

- 0. At the top of the first page that you will be scanning and uploading to Gradescope, write the following statement and sign your name to it: "I will abide by the CU Boulder Honor Code on this exam." FAILURE TO INCLUDE THIS STATEMENT AND YOUR SIGNATURE MAY RESULT IN A PENALTY.
- 1. [2360/072823 (25 pts)] Write the word TRUE or FALSE as appropriate. No work need be shown. No partial credit given.
  - (a) The matrix 0 0 1 0 0 is in RREF.
  - (b) The subset W = (m; n) 2

- 6. [2360/072823 (23 pts)] A 500-gallon tank initial contains 50 pounds of salt dissolved in 100 gallons of water. A brine (salt) solution containing 2 pounds of salt per gallon enters the tank at a rate of 20 gallons per minute. The well-mixed solution in the first tank empties into a second 500-gallon tank, which is initially empty, at a rate 20 gallon per minute. The second tank is also being filled with fresh water at a rate of 5 gallons per minute. The well-mixed solution in the second tank drains at a rate of 20 gallons per minute.
  - (a) (4 pts) Find the volumes,  $V_1(t)$  and  $V_2(t)$ , of salt solution in each tank at time t.
  - (b) (15 pts) Set up, but **do not solve**, the initial value problem describing the amount of salt in each tank as a function of time. Write your final answer using matrices and vectors.
  - (c) (4 pts) Over what time interval is the system of differential equations valid?

Short table of Laplace Transforms: $\angle ff(t)g = F(s) = e^{-st}f(t) dt$ In this table, <i>a</i> ; <i>b</i> ; <i>c</i> are real numbers with <i>c</i> = 0, and <i>n</i> = 0; 1; 2; 3;