APPM 2350-Final Exam Saturday April 30th, 10:30am-1pm 2022

This exam has 5 problems. Please start each new problem at the top of a new page in your blue book. Sho all your work in your blue book and simplify your answers. Answers with missing or insuffcient justification will receive no points. You are allowed one 8.5x11-in page of notes (TWO sided). You may NOT use a calculator, smartphone, smartwatch, the Internet or any other electronic device.

Problem 1(30 points) The following questions are not related:

(a) Find the value(s) and and bwhere the function

$$I(a;b) = \int_{a}^{b} (-2x^2 + 10x - 12)dx$$

has a local maximum. Be sure to support your answer using Calculus 3 concepts.

(b) Consider the function

$$f(x; y; z) = x^2y - z \cos(y)$$

Use a directional derivative to approximate how thurst ges if one moves a distence on the point (4; 0, 3) straight toward the origin.

(c) Arrange the following three double integrals in order from leastated@repalaestjustify your reasoning

Problem 2(30 points)
Given the force vector feld

$$F(x; y; z) = 2$$

Problem 4(20 pts)

The following questions are not related:

(a) Suppose

$$4y \, dx + 7x \, dy = 13$$

C

where C is a simple, smooth curve oriented counter-clockwise iplate that encloses the region R. Given only this information, is it possible to find the reasoning. If not, explain what additional information you'd need.

(b) Let dA give the area of a region the frst quadrant of the plane. (Note, this region is not related to the region part (a)). You are interested in finding themeV, generated by revolving about the x-axist g(x; y) dA is the integral that calculates dibeneV, determine the integral ody).

Problem 5(40 pts)

Consider the 3D solid object is bounded on the $top \pm y^2$, on the bottom by 0 and on the sides by $x^2 + y^2 + z^2 = 8$ Let

$$G = yi - xj + 3zk$$

- (a) Sketch and shade a cross section of the object pilaties Label axes and any intercepts.
- (b) Calculate the volume of the object.
- (c) Calculate the outward fux of the vector the bujuston appropriate Calculus 3 theorem.
- (d) Verify your answer to part (c) by separately calculating the fux through each part of the bounding surface (i.e. the top, the bottom and the side) and adding them together.

End Of Exam: Have a great summer!