

1. (34 pts) Evaluate the following integrals and simplify your answers.

(a) $\int \tan^2 x + 1 \sec^2 x \, dx$

(b) $\int \frac{2x^2 - 5x + 6}{x^3 + 3x} \, dx$

(c) $\int \frac{dx}{x^2 \sqrt{25 - x^2}}$

2. (26 points) Consider the integral $I = \int_1^1 (2 - x)e^x \, dx$.

- (a) Estimate the value of I using the trapezoidal approximation T_2 . Express your answer in terms of the number e and simplify.
- (b) Estimate the error for the approximation T_2 . Express your answer in terms of the number e and simplify.
- (c) Find the exact value of the integral.

3. (22 points) Determine whether the following integrals are convergent or divergent. Explain your reasoning fully for each integral. **If the integral converges, find its value.**

(a) $\int_1^1 x^2 = 3x + 9$.

R. Shade in the region R .

evaluate, an integral to find the volume of the solid

