APPM 1350 Spring 2022

Exam 3

Instructions:

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- This exam has four problems on pages numbered 1 through 9. Make sure you have all pages.
- Write your name and section number at the top of each page.
- Show all work and simplify your answers, except where the instructions tell you to leave your answer unsimplified.
- Name any theorem that you use and explain how it is used.
- Answers with no justification will receive no points unless the problem explicitly states otherwise.
- Notes, your text and other books, calculators, cell phones, and other electronic devices are not permitted, except as needed to upload your work.
- When you have completed the exam, go to the scanning section of the room and upload r2npthe states otherwise.

1. (40 pts)

(a) Evaluate the integral if it exists. 3x + 9

i.
$$p = \frac{3x + 9}{x^2 + 6x} dx$$

ii. $\frac{1}{2} 2 \sin(v) \cos(v) dv$
iii. $\frac{3}{3} (j2x + 4j + 3x)$

(b) $\frac{1}{\frac{3}{4}} \cos(2x) dx = \frac{4}{2} \sin(2x)$ $= \frac{2}{10} \sin(2x)$ $= \frac{2}{10} \sin(2x)$ $= \frac{2}{10}$ (c) Since g is odd $\int_{5}^{5} g(x) dx = 0.$ $\int_{5}^{2} g(x) dx + \int_{2}^{0} g(x) dx + \int_{0}^{5} g(x) = 0$ $\int_{5}^{2} g(x) dx = 14$

Name .

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2. (12 pts)

A fence is to be built to enclose a rectangular area of 250 square feet. The fence along three sides is to be made of material that costs 6 dollars per foot. The material for the fourth side will cost 10 dollars per foot. Find the dimensions of the enclosure that minimize the cost of fencing material.

Solution:

Let x be the width and y be the length of the enclosed area, and suppose that one of the sides of length y costs \$10. The two equations we have are:

$$A = xy = 250 \tag{1}$$

C=6(2x)

3. (24 pts)

- (a) Suppose an object moves with velocity $v(t) = 2t^2 12t + 16$ km/hr along a straight road.
 - i. Determine the displacement of the object on the time interval [1,3].
 - ii. Determine the distance traveled on the time interval [1,3].
- (b) Apply Newton's method to the equation $x^3 + x = 5 = 0$. Use an initial guess of $x_0 = 1$ and find x_1 . (Find only x_1 .)

Solution: X+

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(b) $f(x) = x^3 + x$ 5 and $f^{\emptyset}(x) = 3x^2 + 1$.

$$x_{1} = x_{0} \quad \frac{f(x_{0})}{f^{\emptyset}(x_{0})}$$

= 1 $\frac{1+1}{3+1}$
= 1 + 34
= $\frac{7}{4}$

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4. (24 pts)

- (a) Evaluate the Riemann sum for $f(x) = x^2$ 3 taking the sample points to be right endpoints, a = -4, b = 2 and n = 6.
- (b) Express the integral $\int_{4}^{2} x^2 = 3 dx$ as a limit of Riemann sums. You are not required to fully simplify this expression.
- (c) Evaluate the expression that you gave in (b). Show all steps to find the limit of the Riemann sums.

Solution:

(a) With a = -4; b = 2; n = 6, $x = \frac{2}{6} = 1$. We make a table:

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