- 1. The following are unrelated: (15 pts)
 - (a) Rewrite each of the following without the absolute value symbol:

i. *j*2 6*j*

Solution:

Since
$$> 3, 2 > 6, 2 6 > 0$$
 so $j2 6j = 2 6$

$$6 > 0$$
 so $\frac{7}{2}$

$$6j = 2$$
 6

ii.
$$\int_{0}^{\infty} \overline{2}$$
 2j

Solution:

Since
$$\sqrt[p]{2} < 2$$
, $\sqrt[p]{2}$ $2 < 0$ hence $\sqrt[p]{2}$ $2j = \boxed{} \sqrt[p]{2}$ or $2/2$

(d) Add and simplify: $\frac{2}{\frac{9}{7}} + \frac{5}{12} + 7^0$

Solution:

$$\frac{2}{\frac{9}{7}} + \frac{5}{12} + 7^0 = \frac{14}{9} + \frac{5}{12} + 1$$

$$= \frac{56}{36} + \frac{15}{36} + \frac{36}{36}$$

$$= \boxed{\frac{107}{36}}$$
(4)
$$(5)$$

$$= \boxed{\frac{107}{36}} \tag{6}$$

(e) Simplify: $\frac{j - 7 - 3j + j2j}{2j - 4j}$

Solution:

$$\frac{j}{2j} \frac{7}{4j} \frac{3j + j2j}{8} = \frac{10 + 2}{8}$$

$$= \frac{12}{8}$$

$$= \left[\frac{3}{2}\right]$$
(7)
(8)

2. The following are unrelated. Leave your answers without negative exponents. (20 pts)

(a)
$$(5b^3)^27a^3a^6$$

Solution:

$$(5b^3)^2 7a^3 a^6 = (5)^2 (b^3)^2 7a^3$$
 (10)

$$= 25b^67a^3 (11)$$

$$= \boxed{175b^6a^3} \tag{12}$$

(b) Simplify:
$$\frac{\cancel{D}_{32x^2}}{\cancel{2}_{16}}$$

Solution:

$$\frac{P}{P} \frac{32x^2}{2P} = \frac{jx_j}{16} = \frac{jx_j}{2} \frac{7}{4}$$
 (13)

$$=\frac{jx/4}{2^{D}\overline{2}}$$
 (14)

$$= \boxed{2jxj} \tag{15}$$

(c) Simplify:
$$\frac{2(x^2y^3)^3}{8x^3y^{1-3}}$$

Solution:

$$\frac{2(x^{2}y^{3})^{3}}{8x^{3}y^{1=3}} = \frac{2x^{6}y^{9}}{8x^{3}y^{1=3}}$$
 (16)

$$=\frac{x^{3}y^{\frac{27}{3}}}{4y^{\frac{1}{3}}}\tag{17}$$

$$= \sqrt{\frac{y^{\frac{28}{3}}}{4x^3}} \tag{18}$$

(d) Multiply to rewrite as a polynomial: $\frac{D}{x} = 1 + 3$ $\frac{D}{x} = 1 + 3$

Solution:

(b) Simplify the compound fraction: $\frac{\frac{3}{x^2} - \frac{1}{x}}{\frac{9}{x^2} - 1}$

Solution:

$$\frac{\frac{3}{x^2} + \frac{1}{x}}{\frac{9}{x^2} + 1} = \frac{\frac{3}{x^2}}{\frac{9}{x^2}}$$
 (27)

$$=\frac{3}{9}\frac{x}{x^2} \tag{28}$$

$$=\frac{3 x}{(3 x)(3 + x)} \tag{29}$$

$$= \frac{3}{9} \frac{x}{x^{2}}$$

$$= \frac{3}{(3} \frac{x}{x)(3+x)}$$

$$= \frac{1}{3+x}$$
(28)
(29)

(c) Factor by grouping: $9x^3$ $18x^2$ 4x + 8

Solution:

$$9x^3 18x^2 4x + 8 = 9x^2(x 2) 4(x 2)$$
 (31)

$$= (x \quad 2)(9x^2 \quad 4) \tag{32}$$

$$= (x 2)(9x^{2} 4) (32)$$

$$= (x 2) (3x)^{2} 2^{2} (33)$$

$$= (x - 2)(3x + 2)(3x - 2)$$
 (34)

5. Is x = 2 a solution of the inequality $x^3 2x < 2$

7. Solve each of the following equations. If there are no solutions write NO SOLUTIONS: (10 pts)

(a)
$$\sqrt[p]{8} y + 2 = y 4$$

Solution:

$$8 \quad y = y \quad 6 \tag{41}$$

$$8 \quad y = y^2 \quad 12y + 36 \tag{42}$$

$$y^2 \quad 11y + 28 = 0 \tag{43}$$

$$y^2$$
 11y + 28 = 0 (43)
(y 7)(y 4) = 0 (44)

$$y = 4.7 \tag{45}$$

Plugging into the original equation, we find y = 4 to be extraneous. Hence y = 7

(b) Solve for h: P = A + hdg

Solution:

$$P = A + hdg (46)$$

$$hdg = P \quad A \tag{47}$$

$$h = \boxed{\frac{P - A}{dg}} \tag{48}$$

8. Solve the following inequalities. Justify your answers by using a number line or sign chart if needed. Answers without full justification will not receive full credit. Express all answers in interval notation. (8 pts)

(a)
$$3x + 1 < 6$$

Solution:

$$3x + 1 < 6$$
 (49)

$$3x < 5 \tag{50}$$

$$x > \frac{5}{3} \tag{51}$$

Hence the interval of solution is

(b)
$$x^3 3x^2 0$$

Solution:

We start by factoring the left hand side, and then make use of a number line/sign chart to choose the relevant interval of solution

$$x^3 3x^2 0$$
 (52)

$$x^2(x - 3) = 0$$
 (53)

Setting the left side equal to zero we get two values that make the left side zero: x = 0 and x = 3. Placing these on a number line and picking test values we obtain the following chart



Notice that x = 0 is a solution. Hence the solution is 0 [3; 7].

9. Find all the solutions to the following equation, including the complex solutions (Hint: factoring will be important) $z^3 = 1$. (5 pts)

Solution:

$$z^3 1 = 0 (54)$$

$$z^3$$
 1 = 0 (54)
(z 1)($z^2 + z + 1$) = 0 (55)

From which we conclude that z = 1 or

$$Z = \frac{1}{2} \frac{P \overline{(1)^2 - 4(1)(1)}}{2(1)}$$

$$= \frac{1}{2} \frac{P \overline{(3)}}{2}$$
(56)

$$=\frac{1}{2} \frac{\beta - \overline{3}}{2} \tag{57}$$

$$=\boxed{\frac{1}{2}}$$
 (58)