

Applied Analysis Preliminary Exam

10.00am{1.00pm, August 21, 2019

Instructions: You have three hours to complete this exam. Work all ve problems; each is worth 20 points. Please start each problem on a new page. Please clearly indicate any work that you do not wish to be graded (e.g., write SCRATCH at the top of such a page). You MUST prove your conclusions or show a counter-example for all problems unless otherwise noted. In your proofs, you may use any major theorem on the syllabus or discussed in class, unless you are being asked to prove such a theorem (when in doubt, ask the proctor). Write your student number on your exam, not your name.

Problem 1: Let $\{x_n\}$, $\{a_n\}$, and $\{b_n\}$ be sequences in \mathbb{R} .

(a) Suppose $x_n \rightarrow x$